

Chapter 3: Equations

Properties of equality

1) If $a=b$ then $a = b$
ex: $6 = 6$

2) If $a=b$ then $a = b$
ex: $6 = 6$

3) If $a=b$ then $a = b$
ex: $6 = 6$

4) If $a=b$ then $a = b$
ex: $30 = 30$

(SOLVE)

1st Step Problems

Addition

$$x + 6 = 8$$

Subtraction

$$x - 8 = 4$$

Multiplication

$$-5x = 35$$

Division

$$\frac{x}{3} = -8$$

Cross Multiplication

$$4x = \frac{2}{3}$$

$$\frac{2x}{5} = \frac{4}{10}$$

SOLVING AN EQUATION

2 STEP PROBLEMS

TO SOLVE AN EQUATION MEANS TO FIND THE VALUE OF THE VARIABLE.

ex: 1) $3x - 2 = 10$

2) $4 = 10 - 3x$

3) $\frac{4x + 2}{5} = 10$

4) $-12x + 4 = 16$

5) $\frac{x + 3}{2} = -1$

6) $3(x + 4) = 24$

Part 3: Solving by combining
Like Terms

ex:

1) $4x - 2x = 8$

2) $2x - 8 = 4x - 10$

3) $3x - 7.2 + 2x = 4.8 - x$

4) $-14 = -(-2x + 4)$

5) $3(x + 2) - 2(x - 3) = 14$

PART 4: DISTRIBUTION & CROSS
MULTIPLICATION

1) $3(x-1)=15$

2) $2(x+3)-4(x-2)=100$

3) $\frac{x}{6} = \frac{3}{2}$

4) $\frac{3x+5}{4} = \frac{7}{2}$

5) $\frac{4(x-2)}{3} = \frac{2(x+2)}{5}$

SOLVING EQUATIONS WITH FRACTIONS

$$1) \quad \frac{4x}{9} + \frac{5x}{12} = \frac{31}{36}$$

$$2) \quad \frac{x+2}{7} - \frac{x+3}{2} = \frac{3}{14}$$

3)

$$\frac{x-9}{4} + 3 = \frac{x+2}{6}$$

4)

$$\frac{1}{3} \left(x - \frac{1}{2} \right) - \frac{1}{4} \left(x - \frac{1}{3} \right) = \frac{1}{3}$$

Mathematical Phrases

1. 6 is added to 4
2. a number increased by 6
3. a number tripled
4. a number plus twice the number
5. a number is decreased by 1
6. a number plus a number tripled is 8
7. the difference between a number and 16 is 20
8. 4 more than a number is 16
9. 4 times more than a number is 20
10. the quotient of a number and 8 is 2

Word Problems

1. The sum of twice a number and 4 is 14. Find the number.
2. The quotient of a number and 4 is 8. Find the number.
3. If a number is multiplied by 6 and 10 is added to the product, the result is 76.
Find the number.